



MATH 1030/1040 - Factoring Review

Factoring: follow these steps for every problem

1. Look to see if there is a GCF (greatest common factor):

Ex: $4x^2 - 10xy$
 $2x(2x - 5y)$

2. Look to see if the polynomial is the difference of 2 perfect squares: $x^2 - y^2 = (x + y)(x - y)$

Ex: $4x^2 - 25y^2$
 $(2x + 5y)(2x - 5y)$

3. Look to see if the polynomial is the difference of 2 perfect cubes: $x^3 - y^3 = (x - y)(x^2 + xy + y^2)$

Ex: $x^3 - 8$
 $(x - 2)(x^2 + 2x + 4)$

4. Look to see if the polynomial is the sum of 2 perfect cubes: $x^3 + y^3 = (x + y)(x^2 - xy + y^2)$

Ex: $27y^3 + 64$
 $(3y + 4)(9y^2 - 12y + 16)$

5. If trinomial, break into 2 binomials:

Ex: $x^2 - 19x + 48$

$(x \quad) (x \quad)$ Determine the front (first) terms;
 $(x - \quad) (x - \quad)$ Determine the SIGNS;
Determine the back (last) terms – by listing the factors.
Factors of 48: 1, 48; 2, 24; 3, 16; 4, 12; 6, 8
 $(x - 16)(x - 3)$ Find pair that adds to 19 => 3+16 add to 19

6. If the polynomial has 4 terms, use grouping:

Ex: $\underline{x^3 + 2x^2} \quad \underline{- 9x - 18}$ No GCF for all 4 terms

↓ ↓
Factor Factor

$\underline{\underline{x^2(x + 2) - 9(x + 2)}}$ *now factor GCF binomial

↓
 $(x + 2)(x^2 - 9)$ Difference of 2 perfect squares

↓
 $(x + 2)(x + 3)(x - 3)$